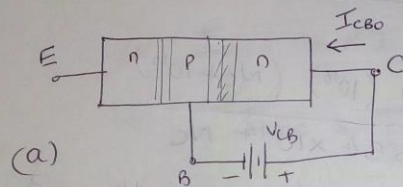
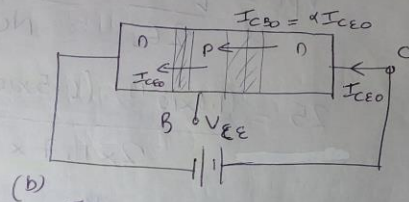


⇒ 2nd breakdown mechanism (Avalanche breakdown)



(a)  $BV_{CB0}$  is breakdown voltage of CB junction



(b) For  $I_B = 0$ , breakdown voltage (ie Base open) at  $V_{CE}$  is called  $BV_{CE0}$

- fig 6a) Open emitter configuration with saturation current  $I_{CBO}$   
 b) Open Base configuration with saturation current  $I_{CEO}$

Fig (6a) is an npn BJT with a R.B  $V_{BC}$  applied 35 and with emitter left open. The current  $I_{CBO}$  is the R.B junction current.

Fig (6b) shows npn BJT with an applied  $V_{CE}$  and base left open.

This bias condition also makes the BC junction reverse-biased.

The current  $I_{CBO}$  in fig (6b) is the normal R.B BC junction current. Part of this current is due to flow of minority carriers holes from the collector across the BC depletion region into the base.

Note: (Flow of holes into the base makes Base +ve w.r.t emitter) and BE junction  $\Rightarrow$  F.B, which produces  $I_{CE0}$ , due to injection of  $e^-$ s from E into Base.

The injected  $e^-$ s diffuse across the base towards the BC junction where it becomes  $\alpha I_{CE0}$ .

$$\therefore I_{CE0} = \alpha I_{CE0} + I_{CBO} \quad \text{--- (1)}$$

$$\therefore I_{CE0} \approx \frac{I_{CBO}}{1-\alpha} \approx \beta I_{CBO} \quad \text{--- (2)}$$

Note:

$$\beta = \frac{\alpha}{1-\alpha} \approx \frac{1}{1-\alpha}$$

Thus the R.B junction current  $I_{CBO}$  is multiplied by the current gain  $\beta$  when the transistor is biased in the open-base configuration.

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- When Transistor is biased in open-emitter configuration <sup>36</sup> as in fig 6(a), current  $I_{CBO}$  at breakdown becomes  $I_{CEO} \rightarrow M I_{CBO}$ ; where  $M$  is the multiplication factor.

$$M = \frac{1}{1 - \left(\frac{V_{CB}}{BV_{CBO}}\right)^m} \quad \text{--- Empirical approximation for } M. \quad \text{--- (3)}$$

where,  $m$  is an empirical constant ( $3 < m < 6$ ) and  $BV_{CBO}$  is B-C breakdown voltage with the emitter left open.

- When transistor is biased with base open; currents in B-C junction at breakdown are multiplied, so that  $I_{CEO} = M(\alpha I_{CEO} + I_{CBO})$

Solving for  $I_{CEO} \Rightarrow I_{CEO} \approx \frac{M I_{CBO}}{1 - \alpha M}$

Thus condition for breakdown corresponds to

$$\alpha M = 1 \quad \text{--- (4)}$$

$$M = \frac{1}{\alpha}$$

$$\Rightarrow \frac{1}{1 - \left(\frac{BV_{CEO}}{BV_{CBO}}\right)^m} = 1 \quad \text{(using (3) \& (4))}$$



where,  $BV_{CEO}$  is the C-E voltage at breakdown  $BV_{CBO}$  in open base mode.

$$\Rightarrow \frac{BV_{CEO}}{BV_{CBO}} = (1-\alpha)^{1/m} \quad \text{--- ( } \beta = \frac{\alpha}{1-\alpha} \text{ )}$$

$\therefore$   $BV_{CEO} = \frac{BV_{CBO}}{(1+\beta)^{1/m}}$  ---> Relation bet<sup>n</sup>  $BV_{CEO}$  &  $BV_{CBO}$ .  
--- (A)

i.e.  $BV_{CBO} \gg BV_{CEO}$

Note:

→ In a transistor CRT, the transistor must be designed to operate under a worst-case situation (eg breakdown) i.e why we designer's should know the upper & lower limit of breakdown voltages (ie  $BV_{CEO}$  &  $BV_{CBO}$ )

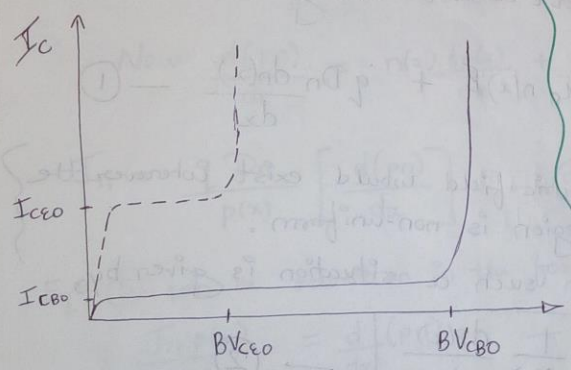


fig (d) Relative breakdown voltages and saturation currents of the open base and open emitter configuration.

• It means that  $BV_{CEO}$  is small by the factor  $\frac{1}{\sqrt{1+\beta}}$  than the actual avalanche junction breakdown voltage.

\*

## Gummel-Poon model:

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• Gummel-Poon model takes into account the in-depth picture of physical processes taking place within a BJT and is therefore quite capable of handling non-ideal situations (such as non-uniform doping concentration in the base).

• Let us consider an npn transistor.

The minority carrier current density in the base region is,

$$J_n = q \mu_n n(x) E + q D_n \frac{dn(x)}{dx} \quad \text{--- (1)}$$

{ \* Concept: An Electric field would exist whenever the doping in base region is non-uniform. }

Then, E-field in such a situation is given by,

$$E = \frac{KT}{q} \frac{1}{p(x)} \frac{dp(x)}{dx} \quad \text{--- (2)}$$

where,  $p(x)$  is the majority carrier hole concentration in the base.

• The direction of this E-field is from collector to emitter which will aid the flow of electrons across the base.

Put eq<sup>n</sup> (2) in eq<sup>n</sup> (1), we get

$$J_n = q \mu_n n(x) \frac{kT}{q} \frac{1}{p(x)} \frac{dp(x)}{dx} + q D_n \frac{dn(x)}{dx} \quad \text{--- (3)}$$

From Einstein's relation;  $D_n = V_T \mu_n = \frac{kT}{q} \mu_n$  --- (4)

⇒ So eq<sup>n</sup> (3) becomes,

$$J_n = \frac{q D_n}{p(x)} \left[ n(x) \frac{dp(x)}{dx} + p(x) \frac{dn(x)}{dx} \right]$$

Now  $\frac{d(pn)}{dx} = n(x) \frac{dp(x)}{dx} + p(x) \frac{dn(x)}{dx}$  } → derivative of product.

$$J_n = \frac{q D_n}{p(x)} \left[ \frac{d(pn)}{dx} \right] \quad \text{--- (5)}$$

Eq<sup>n</sup> (5) can be rewritten in the form,

$$\frac{J_n p(x)}{q D_n} = \frac{d(pn)}{dx} \quad \text{--- (6)}$$

Integrating eq<sup>n</sup> (6) across the base-region, while assuming that electron current density is constant (i.e.  $J_n$ ) and  $D_n$  is a constant.

$$\frac{J_n}{q D_n} \int_0^{w_B} p(x) dx = \int_0^{w_B} \frac{d(pn)}{dx} dx = \int_0^{w_B} n(x) \frac{dp(x)}{dx} dx \quad \text{--- (7)}$$



$$\int_0^{w_B} \frac{J_n}{q D_n} p(x) dx = n(w_B) p(w_B) - n(0) p(0) \quad \text{--- (8)}$$

In active mode, BE junction is forward-bias and BC junction is reverse-bias,

we have  $n(0) = n_{B0} e^{\left(\frac{V_{BE}}{V_T}\right)}$ ,  $n(w_B) = 0$  --- (9)

we know,  $p_0 = n_i^2$  --- under equilibrium.

Eq<sup>n</sup> (8) becomes, (using eq<sup>n</sup> (9)), we get

$$\frac{J_n}{q D_n} \int_0^{w_B} p(x) dx = 0 - n_{B0} e^{\frac{V_{BE}}{V_T}} p(0)$$

We know,  $n_{B0} p(0) = n_i^2$

$$\int_0^{w_B} p(x) dx = -n_i^2 e^{\left(\frac{V_{BE}}{V_T}\right)}$$

$$J_n = \frac{-q D_n n_i^2 e^{\left(\frac{V_{BE}}{V_T}\right)}}{\int_0^{w_B} p(x) dx} \quad \text{--- (10)}$$

In above expression of  $J_n$ ,  $\int_0^{w_B} p(x) dx$  is called Gummel number  $Q_B$

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i.e.  $\int_0^{w_B} p(x) dx$  i.e. integral in the denominator is the total integrated majority carrier charge in the base and is known as 'base Gummel number' ( $Q_B$ )

$$Q_B = \int_0^{w_B} p(x) dx \quad \text{--- (11)}$$

A similar analysis in the emitter region results in a hole current density given by,

$$J_p = -q D_p n_i^2 e^{\frac{V_{BE}}{V_T}} \frac{1}{\int_0^{w_E} n(x) dx} \quad \text{--- (12)}$$

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where  $\int_0^{w_E} n(x) dx$  is called the Emitter Gummel number  $Q_E$ .

Gummel-Poon model can also take into account non-ideal effects, such as the "Early effect" and "high-level injection."



Extra!

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+R  
• As B-C voltage changes, neutral base width  $W_B$  changes so that  $Q_B$  changes.

The change in  $Q_B$  with B-C voltage then makes  $I_n$  (equation (10)) a function of B-C voltage.

This is the "base-width modulation" or "Early effect".

• If  $V_{BE}$  becomes too large, low-level injection no longer applies, which leads to high-level injection.

• In this case, the total hole concentration in base  $\uparrow$ ses because of  $\uparrow$ sed excess hole concentration.

This means that  $Q_B \uparrow$ ses (from eq<sup>n</sup> (11)),

ie  $I_n$  will also change (from eq<sup>n</sup> (10)).

∴ The Gummel-Poon model can then be used to describe the basic operation of BJT as well as to describe non-ideal effects.

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