

Threshold voltage of a MOS device:-

V_{TO} : It is defⁿ as min gate v_{tg} V_G req^d to cause surface inversion when substrate bias $V_{SB} = 0$.

$$V_{TO} = \underbrace{\phi_{GC} - 2\phi_F}_{\text{For Ideal mos device}} - \underbrace{\frac{Q_{Bo}}{C_{ox}} - \frac{Q_{ox}}{C_{ox}} - \frac{Q_{ss}}{C_{ox}}}_{\text{due to process non-linearity}} \text{ Volts}$$
$$= V_1 + V_2 + V_3 + V_4 + V_5.$$

OR

Threshold voltage is that value of gate voltage for which the channel is depleted of majority carriers.

For all practical purposes, we can identify four physical components of V_T :-

- 1) $\phi_{GC} \rightarrow$ work funⁿ diff betⁿ gate & channel.
- 2) Gate voltage component to change the surface potential.
- 3) Gate v_{tg} compⁿ to offset the fixed charges in gate oxide and in Si-oxide interface.
- 4) gate v_{tg} compⁿ to offset depletion region charge.

V_1 :-

When a MOS device is formed, there exist a contact potential across the MOS device due to work funⁿ difference betⁿ the metal gate and Si substrate.

$$V_1 = \frac{\phi_{GC}}{\phi_{F(\text{substrate})} - \phi_m} \rightarrow \text{for metal gate}$$

$$V_1 = \frac{\phi_{GC}}{\phi_{F(\text{substrate})} - \phi_m} \text{ or } \phi_{ms}$$

$$V_1 = \frac{\phi_{Fsub} - \phi_{Fgate}}{\phi_{FP} - \phi_{FN}}$$

for Poly Si gate
Select 0.55V
for metal gate / Poly Si gate

doping will be in numerical.
↓
Calculate $\phi_{gate} = \phi_m$ from formula

→ V_2 :

The change in gate v_{tg} req'd to create a ~~depletion~~ ^{inversion} layer having thickness x_{dm}

$$V_2 = \phi_s - \phi_f \text{ (refer E.B.D)}$$

$$V_2 = -\phi_f - \phi_f \quad \because \phi_s = \phi_f$$

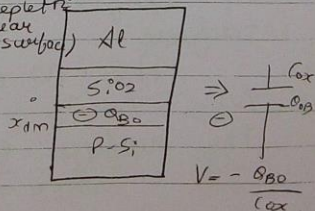
$$V_2 = -2\phi_{Fsub} \text{ Volts.}$$

↓
To achieve surface inversion, i.e. to change ext^r gate v_{tg} must be changed the surface potential by $-2\phi_f$.

→ V_3 :

The gate v_{tg} req'd to offset the effect of depletion charge density Q_{B0} C/cm^2 is (which is due to fixed acceptor ions located in depletion region near the surface)

$$V_3 = -\frac{Q_{B0}}{C_{ox}} \text{ Volts.}$$



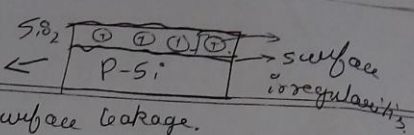
$$Q_{B0} = -\sqrt{2q N_A \cdot \epsilon_{si} | -2\phi_f |}$$

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leads to some charges called V_4 :- surface charges \rightarrow cause surface leakage.

The gate v_{tg} need to offset the effect of this fixed oxide layer charge is

$V_4 = - \frac{Q_{ox}}{C_{ox}}$ Volts.



• Due to process non-linearity, there are a fixed no of oxide layer charges N_{ox}/cm^2 . The fixed oxide layer charge density N_{ox}

$$Q_{ox} = q N_{ox} \quad C/cm^2$$

C_{ox} : gate oxide Capacitance per unit area

$$C_{ox} = \frac{\epsilon_{ox}}{t_{ox}}$$

\rightarrow There always exists a fixed +ve charge density Q_{ox} at interface betn gate oxide & Si substrate, due to impurities and/or lattice imperfections at the interface.

$\rightarrow V_5$: Due to process non-linearities, there are surface charges present at Si-SiO₂ interface.

The no of surface charges is N_{ss}/cm^2 . The surface charge density is $Q_{ss} = q N_{ss} \quad C/cm^2$

The gate vty reqd to offset the effect of Q_{ss} is

$$V_5 = -\frac{Q_{ss}}{C_{ox}} \text{ Volts.}$$

Hence total gate vty reqd to create an inversion layer is the sum of above 5 voltages,

$$V_{TO} = V_1 + V_2 + V_3 + V_4 + V_5$$

$$V_{TO} = \phi_{GC} - 2\phi_F - \frac{Q_{BO}}{C_{ox}} - \frac{Q_{ox}}{C_{ox}} - \frac{Q_{ss}}{C_{ox}}$$

↳ Valid for NMOS & PMOS

↳ Threshold voltage of a MOS device for Zero Substrate bias $V_{SB} = 0$

Q1. For an NMOS T^r , substrate doping density $N_A = 10^{16}/\text{cm}^3$, gate oxide thickness $t_{ox} = 500 \text{ \AA}$, no of fixed oxide charges $N_{ox} = 2 \times 10^{10}/\text{cm}^2$, no of surface charges $N_{ss} = 0$. Find V_{TO} if $V_{SB} = 0$.

Data: -

$$\begin{aligned} N_A &= 10^{16}/\text{cm}^3 \\ t_{ox} &= 500 \text{ \AA} \\ N_{ox} &= 2 \times 10^{10}/\text{cm}^2 \\ N_{ss} &= 0, V_{SB} = 0 \end{aligned}$$

$$\begin{aligned} n_i &= 1.45 \times 10^{10} \text{ cm}^{-3} \\ \epsilon_{Si} &= 11.7 \times 8.854 \times 10^{-14} \text{ F/cm} \\ \epsilon_{ox} &= 3.97 \times 8.854 \times 10^{-14} \text{ F/cm} \end{aligned}$$

To find: -
 $V_{TO} = ?$

$$\text{Soln: - } V_{TO} = \phi_{GC} - 2\phi_F - \frac{Q_{BO}}{C_{ox}} - \frac{Q_{ox}}{C_{ox}} - \frac{Q_{ss}}{C_{ox}}$$

• $\phi_{GC} \Rightarrow$

$$\phi_{GC} = \phi_{Fsub} - \phi_{Fgate}$$

$$\phi_{Fsub} = \frac{kT}{q} \ln \left[\frac{n_i^2}{N_A} \right]$$

$$= 0.026 \ln \left[\frac{1.45 \times 10^{10}}{10^{16}} \right] = -0.35V$$

Select $\phi_{Fgate} = 0.55V$

$$\therefore \phi_{GC} = -0.35 - 0.55$$

$$= -0.9V //$$

• $Q_{Bo} = -\sqrt{2q \epsilon_{si} N_A | -2\phi_F |} \quad C/cm^2$

$$= -\sqrt{2 \times 1.6 \times 10^{-19} \times 11.7 \times 8.854 \times 10^{-14} \times 10^{16} \times 0.7}$$

$$= -48.17 \times 10^{-9} \quad C/cm^2 //$$

• $Q_{ox} = q N_{ox} \quad C/cm^2$

$$= 1.6 \times 10^{-19} \times 2 \times 10^{10}$$

$$= 3.2 \times 10^{-9} \quad C/cm^2 //$$

• $Q_{ss} = q N_{ss}$

$$= 0 \quad C/cm^2 //$$

• $C_{ox} = \frac{\epsilon_{ox}}{t_{ox}}$

$$= \frac{8.854 \times 10^{-14} \times 3.97}{500 \times 10^{-8}}$$

$$= 70.3 \times 10^{-9} \quad F/cm^2$$

$$V_{T0} = \phi_{GC} - 2\phi_F - \frac{Q_{Bo}}{C_{ox}} - \frac{Q_{ox}}{C_{ox}} - \frac{Q_{ss}}{C_{ox}}$$

$$= -0.4 - 2(-0.35) + \frac{48.17}{70.3} - \frac{3.2}{70.3} - 0$$

$$V_{T0} = 0.44 \text{ Volts}$$

↳ (For NMOS, V_{T0} is +ve)

Q2 For a PMOS TR, $N_D = 10^{16}/\text{cm}^3$,
 $t_{ox} = 500 \text{ \AA}$, $N_{ox} = 2 \times 10^{10}/\text{cm}^2$,
 $N_{ss} = 0$, $\psi_B = 0$. Find V_{T0} .

Soln: - $V_{T0} = \phi_{GC} - \phi_F - \frac{Q_{Bo}}{C_{ox}} - \frac{Q_{ox}}{C_{ox}} - \frac{Q_{ss}}{C_{ox}}$

• $\phi_{GC} = \phi_{Fsub} - \phi_{Fgate}$

$$\phi_{Fsub} = \frac{kT}{q} \ln \left[\frac{N_D}{n_i} \right]$$

$$= 0.35 \text{ V}$$

Select $\phi_{Fgate} = 0.55 \text{ V}$

∴ $\phi_{GC} = 0.35 - 0.55 \text{ V}$
 $= -0.2 \text{ V}$

• $Q_{Bo} = \sqrt{2q N_D \epsilon_{Si} | -2\phi_F |}$
 $= 48.17 \times 10^{-9} \text{ C/cm}^2$

• $Q_{ox} = q N_{ox}$
 $= 1.6 \times 10^{-19} \times 2 \times 10^{10} = 3.2 \times 10^{-9} \text{ C/cm}^2$

• $C_{ox} = \epsilon_{ox}/t_{ox} = 70.3 \times 10^{-9} \text{ F/cm}^2$

• $Q_{ss} = q N_{ss} = 0$

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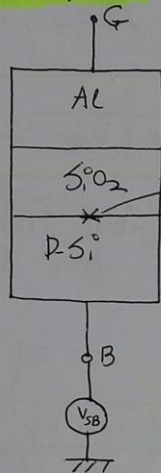
$$\begin{aligned}
 \cdot V_{TO} &= \phi_{gc} - 2\phi_F - \frac{Q_{BO}}{C_{oxc}} - \frac{Q_{ox}}{C_{oxc}} - \frac{Q_{ss}}{C_{oxc}} \\
 &= -0.2 - 0.7 - \frac{48.17}{70.3} - \frac{3.2}{70.3} - 0
 \end{aligned}$$

$$V_{TO} = -1.63 \text{ Volts.}$$

↳ For PMOS V_{TO} is -ve.

Note: Voltage drop across the depletion region at inversion is $-2\phi_F$

→ **Threshold voltage (V_T):**
if $V_{SB} \neq 0$.



Surface potential at Si-SiO₂ interface changes to $\phi_s + V_{SB}$

• Effect of V_{SB} :

→ Surface potential changes to $\phi_s + V_{SB}$

→ Depletion charge density change to Q_B

$$Q_{B0} = -\sqrt{2q\epsilon_{Si} N_A | -2\phi_F |} \quad \text{C/cm}^2$$

$$Q_B = -\sqrt{2q\epsilon_{Si} N_A | -2\phi_F + V_{SB} |} \quad \text{C/cm}^2$$

→ Threshold v_{tg} changes to V_T

$$V_T = \phi_{GC} - 2\phi_F - \frac{Q_B}{C_{ox}} - \frac{Q_{ox}}{C_{ox}} - \frac{Q_{ss}}{C_{ox}}$$

↳ V_T if $V_{SB} \neq 0$

Note:-

$$V_T = \phi_{GC} - 2\phi_F - \frac{Q_{B0}}{C_{ox}} - \frac{Q_{ox}}{C_{ox}} - \frac{Q_{ss}}{C_{ox}} - \left(\frac{Q_B - Q_{B0}}{C_{ox}} \right)$$

$$V_T = V_{T0} - \frac{Q_B - Q_{B0}}{C_{ox}}$$

$$\gamma = 0.819 \quad \underline{V^{1/2}}$$

$$V_T = V_{T0} + \gamma \left[\sqrt{|-2\phi_F + V_{SB}|} - \sqrt{|-2\phi_F|} \right]$$

$$V_T = 0.44 + 0.819 \left[\sqrt{|10.7+2|} - \sqrt{|10.7|} \right]$$

$$V_T = \underline{1.10 \text{ Volts}}$$

Q4. w.r.t Q(2), if $V_{SB} = -1V$, find V_T

- Solⁿ: $V_T = -1.632 V$ (Refer Q2)

$$\gamma = -\sqrt{\frac{2q E_{Si} N_D}{\epsilon_{Si}}} \quad (V^{1/2})$$

$$\gamma = -0.819 \quad \underline{V^{1/2}}$$

$$V_T = V_{T0} + \gamma \left[\sqrt{|-2\phi_F + V_{SB}|} - \sqrt{|-2\phi_F|} \right]$$

$$V_T = \underline{-2.01 \text{ Volts}}$$

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Q. Find depletion layer width (x_d), depletion charge density Q_{BO} , flat band v.t.g V_{FB} threshold voltage V_{TO} with $V_{SB} = 0$ & body factor γ .

Given: - $t_{ox} = 400 \text{ \AA}$ \rightarrow gate oxide thickness

Substrate acceptor doping $N_A = 1.5 \times 10^{16} / \text{cm}^3$

$N_D \rightarrow$ Donor doping concⁿ $N_D = 10^{18} / \text{cm}^3$

$N_{oxc} \rightarrow$ density of singly charged the surface ions is $5 \times 10^{10} / \text{cm}^2$.

$\Rightarrow n_i^0 = 1.45 \times 10^{10} / \text{cm}^3$, $\epsilon_{ox} = 0.345 \times 10^{-12} \text{ F/cm}^2$

$\epsilon_{Si}^0 = 11.7 \epsilon_0 = 1.035 \times 10^{-12} \text{ F/cm}^2 = \epsilon_{ox} \times 3.97$

Soln: - i) $x_d = \sqrt{\frac{2 \epsilon_{Si}^0 | -2\phi_F |}{q N_A}}$

For n-channel MOSFET

$$\phi_{Fsub} = \frac{kT}{q} \ln\left(\frac{n_i^0}{N_A}\right)$$

$$\phi_{Fsub} = -0.36 \text{ V} = \phi_F$$

$$x_d = \sqrt{\frac{2 \epsilon_{Si}^0 | -2\phi_F |}{q N_A}}$$

$$x_d = 24.71 \text{ \AA}$$

$$Q_{BO} = -\sqrt{2q \epsilon_{Si}^0 N_A | -2\phi_F |}$$

$$Q_{BO} = -59.8 \times 10^{-9} \text{ F/cm}^2$$

$$V_{FB} = \phi_{GC} - \frac{Q_{ox}}{C_{ox}}$$

$$\phi_{GC} = \phi_{Fsub} - \phi_{Fgate}$$

$$\Rightarrow \text{let } \phi_{Fgate} = 0.55 \text{ V}$$

$$\therefore \phi_{GC} = -0.36 - 0.55 \\ = -0.91 \text{ V.}$$

$$\bullet Q_{ox} = q N_{ox} = 8 \times 10^{-9} \text{ F/cm}^2$$

$$\bullet C_{ox} = \frac{\epsilon_{ox}}{t_{ox}} = 86.25 \text{ nF/cm}$$

$$\bullet V_{FB} = \phi_{GC} - \frac{Q_{ox}}{C_{ox}} \\ = -0.91 - \frac{8}{86.25} = \underline{\underline{1 \text{ V}}}$$

$$Q_{ss} = 0$$

$$\bullet V_{TO} = \phi_{GC} - 2\phi_F - \frac{Q_{ox}}{C_{ox}} - \frac{Q_{B0}}{C_{ox}} - \frac{Q_{ss}}{C_{ox}} \\ = -0.91 - 2(-0.36) + \frac{59.8}{86.25} - \frac{8}{86.25}$$

$$\boxed{V_{TO} = 0.41 \text{ Volts}}$$

• Body factor :- (γ)

$$\gamma = \frac{\sqrt{2q \epsilon_{si} N_A}}{C_{ox}}$$

$$\boxed{\gamma = 0.817 \text{ V}^{1/2}}$$

$$t_{ox} = 500 \text{ \AA}, N_A = 10^{16} \text{ cm}^{-3}$$