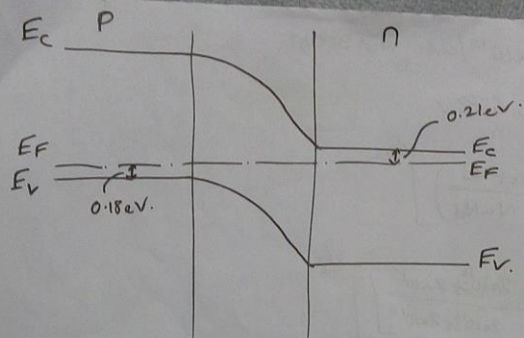


1.



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$$n_0 = N_c \exp\left[-\frac{(E_c - E_F)}{kT}\right]$$

$$N_c = 2.8 \times 10^{19} / \text{cm}^3, N_v = 1.04 \times 10^{19} / \text{cm}^3, kT = \underline{26 \text{ mV}}$$

$$n_0 = 2.8 \times 10^{19} \left[\frac{-(0.21) \text{ eV}}{0.026 \text{ eV}} \right]$$

$$n_0 = N_d = \underline{8.69 \times 10^{15} / \text{cm}^3} \text{ (n-region)}$$

$$p_0 = N_v \exp\left[-\frac{(E_F - E_v)}{kT}\right]$$

$$= 1.04 \times 10^{19} \exp\left[\frac{-0.18 \text{ eV}}{0.026 \text{ eV}}\right]$$

$$p_0 = N_a = \underline{1.02 \times 10^{16} / \text{cm}^3} \text{ (p-region)}$$

$$V_{bi} = V_t \ln\left[\frac{N_a N_d}{n_i^2}\right] = 26 \text{ mV} \times \ln\left[\frac{1.02 \times 10^{16} \times 8.69 \times 10^{15}}{2.25 \times 10^{20}}\right]$$

$$= \underline{0.634 \text{ V}}$$

2. $N_a = 2 \times 10^{16} / \text{cm}^3$, $N_d = 2 \times 10^{15} / \text{cm}^3$, $T = 300\text{K}$

$$V_{bi} = V_T \ln \left[\frac{N_a N_d}{n_i^2} \right] = 0.673\text{V}$$

$$W = \left[\frac{2 \epsilon_s (V_{bi} + V_R)}{q} \left(\frac{N_a + N_d}{N_a N_d} \right) \right]^{1/2}$$

$$= \left[\frac{2 \times 10^{-12} \times (V_{bi} + V_R)}{1.6 \times 10^{-19}} \left[\frac{2 \times 10^{16} \times 2 \times 10^{15}}{2 \times 10^{16} \times 2 \times 10^{15}} \right] \right]^{1/2}$$

$$W = \left[6.875 \times 10^{-9} (V_{bi} + V_R) \right]^{1/2}$$

For $V_R = 0$, $W = 68.02 \times 10^{-6} \text{cm} = \cancel{68.02 \mu\text{m}} = 0.68 \times 10^{-4} \text{cm}$

For $V_R = 8\text{V}$, $W = 2.44 \times 10^{-4} \text{cm} = \underline{244.18 \times 10^{-6} \text{cm}} = \underline{2.44 \times 10^{-4} \text{cm}}$

$$E_m = \left| \frac{2(V_{bi} + V_R)}{W} \right| \rightarrow$$

For $V_R = 0$, $E_m = -19.79 \times 10^4 \text{V/cm}$

For $V_R = 8\text{V}$, $E_m = -71.09 \times 10^3 \text{V/cm}$

3. $N_a = 5 \times 10^{17} / \text{cm}^3$, $N_d = 10^{17} / \text{cm}^3$, $A = 10^{-4} \text{cm}^2$, $V_R = 5\text{V}$.

V_{bi} , x_n , x_p , W , E_m ,

$$\rightarrow V_{bi} = \frac{kT}{q} \ln \left[\frac{N_a N_d}{n_i^2} \right] = \underline{0.858\text{V}}$$

$$W = \sqrt{\frac{2 \epsilon_s (V_{bi} + V_R)}{q} \left(\frac{N_a + N_d}{N_a N_d} \right)} = \sqrt{\frac{2 \times 10^{-12} \times (0.858 + 5)}{1.6 \times 10^{-19}} \left(\frac{5 \times 10^{17} + 10^{17}}{5 \times 10^{17} \times 10^{17}} \right)}$$

$$W = \underline{29.64 \times 10^{-6} \text{cm}}$$

$$|x_n| = \left(\frac{N_a}{N_a + N_d} \right) W = \underline{24.7 \times 10^{-6} \text{cm}}; |x_p| = \left(\frac{N_d}{N_a + N_d} \right) W = \underline{4.94 \times 10^{-6} \text{cm}}$$

$$E_m = -\frac{2(V_{bi} + V_R)}{W} = \underline{-3.95 \times 10^5 \text{V/cm}}$$

$$C_j = \frac{qA}{W} = \frac{(1.7) \times (8.854 \times 10^{-14}) \times 10^{-4}}{29.64 \times 10^{-6}} = 3.37 \times 10^{-12} \text{F} = \underline{3.37 \text{pF}}$$

4. $T = 300\text{K}$, $N_a = 5 \times 10^{15}/\text{cm}^3$, $N_d = 10^{14}/\text{cm}^3$

$$V_{bi} = V_T \ln \left[\frac{N_a N_d}{n_i^2} \right] = 0.559\text{V}$$

$$W = \left[\frac{2 \epsilon_s (V_{bi})}{q} \left(\frac{N_a + N_d}{N_a N_d} \right) \right]^{1/2}$$

$$= \left[\frac{2 \times 10^{-12} \times 0.559}{1.6 \times 10^{-19}} \left[\frac{5 \times 10^{15} + 10^{14}}{5 \times 10^{15} \times 10^{14}} \right] \right]^{1/2} = 266.96 \times 10^{-6} \text{cm}$$

$$x_n = \left(\frac{N_a}{N_a + N_d} \right) W = \frac{261.72 \times 10^{-6}}{\text{cm}}, \quad x_p = \left(\frac{N_d}{N_a + N_d} \right) W = 5.23 \times 10^{-6} \text{cm}$$

5. pn junction diode (Si) at $T = 300\text{K}$.

In forward-bias,

$$I_f = I_s \exp \left(\frac{V_a}{V_T} \right) \quad (\text{neglecting } \epsilon^{-1})$$

Then,

$$\frac{I_{f1}}{I_{f2}} = \frac{I_s \exp \left(\frac{2V_{a1}}{V_T} \right)}{I_s \exp \left(\frac{2V_{a2}}{V_T} \right)} = \exp \left[\frac{2}{V_T} (V_1 - V_2) \right]$$

$$V_{a1} - V_{a2} = (V_T) \ln \left(\frac{I_{f1}}{I_{f2}} \right)$$

a) For $\frac{I_{f1}}{I_{f2}} = 10 \Rightarrow V_{a1} - V_{a2} = 26 \times 10^{-3} \ln [10]$

\therefore Change in diode vtg $(V_{a1} - V_{a2}) = 59.86 \text{ mV}$

6. p⁺n Si diode, $T=300\text{K}$, $N_A=10^{18}/\text{cm}^3$, $N_D=10^{16}/\text{cm}^3$, $D_p=12\text{cm}^2/\text{s}$, $\tau_{p0}=10^{-7}\text{s}$, $A=10^{-4}\text{cm}^2$, $V_a=0.5\text{V}$

Solⁿ:
$$I_s = \frac{q D_n n_{p0}}{L_n} + \frac{q D_p p_{n0}}{L_p}$$

$$I_s = A q n_i^2 \left[\frac{1}{N_A} \sqrt{\frac{D_n}{L_{n0}}} + \frac{1}{N_D} \sqrt{\frac{D_p}{L_{p0}}} \right]$$

For a p⁺n Jⁿ

$$I_s = A q n_i^2 \left[\frac{1}{N_D} \sqrt{\frac{D_p}{L_{p0}}} \right]$$

$$I_s = 10^{-24} \times 1.6 \times 10^{-19} \times 2.25 \times 10^{20} \left[\frac{1}{10^{16}} \sqrt{\frac{12}{10^{-7}}} \right]$$

$$I_s = 3.943 \times 10^{-15} \text{ A}$$

$$I_D = I_s \exp\left(\frac{V_a}{V_T} - 1\right)$$

$$= 3.94 \times 10^{-15} \exp\left[\frac{0.5}{26\text{mV}} - 1\right]$$

$$I_D = 8.85 \times 10^{-7} \text{ A}$$

7. $L_p = 0.2\text{cm}$, $L_n = 0.1\text{cm}$, $A = 10^{-2}\text{cm}^2$, $N_D = 10^{15}/\text{cm}^3$, $N_A = 10^{16}/\text{cm}^3$, $\mu_p = 480$, $\mu_n = 1350\text{cm}^2/\text{V}\cdot\text{s}$

a) p-region:

$$R_p = \frac{\rho_p L}{A} = \frac{L}{\sigma_p A} = \frac{L}{A(q\mu_p N_A)}$$

$$R_p = \frac{0.2}{10^{-2} (1.6 \times 10^{-19} \times 480 \times 10^{16})} = 26 \Omega$$

b) n-region:

$$R_n = \frac{\rho_n L}{A} = \frac{L}{\sigma_n A} = \frac{L}{A(q\mu_n N_D)} = \frac{0.1}{10^{-2} (1.6 \times 10^{-19} \times 1350 \times 10^{15})} = 46.30 \Omega$$

Total series resistance is $R = R_p + R_n = 26 + 46.3 = 72.3 \Omega$

8. $V_a = 20\text{mV}$, $I_s = 10^{-13}\text{A}$

$$\Rightarrow \frac{1}{r_d} = \frac{dI_D}{dV_a} = I_s \left[\frac{1}{V_T} \right] \exp\left(\frac{V_a}{V_T}\right)$$

$$\frac{1}{r_d} = \frac{10^{-13}}{26\text{mV}} \exp\left(\frac{20\text{mV}}{26\text{mV}}\right)$$

$$\Rightarrow r_d = 1.2 \times 10^{11} \Omega$$

$$I_D = I_s \exp\left(\frac{V_a}{V_T}\right)$$

$$\frac{dI_D}{dV_a} = \frac{I_s}{V_T} \exp\left(\frac{V_a}{V_T}\right)$$

9. $V_B = \frac{E_s E_{crit}^2}{2q N_B}$; $E_{crit} = 4 \times 10^5 \text{ V/cm}$, $V_B = 30\text{V}$

$$\rightarrow N_B = \frac{E_s E_{crit}^2}{V_B 2q}$$

$$\therefore N_B = \frac{11.7 \times 8.854 \times 10^{-14} \times (4 \times 10^5)^2}{30 \times 2 \times 1.6 \times 10^{-19}}$$

$$N_D = N_B = 1.73 \times 10^{16} / \text{cm}^3$$

10. Find cut-off freqⁿ of a BJT; f_{ω} & Beta cut-off freq?
 $\tau_{ec} = \tau_D = 104 \times 10^{-12} \text{ sec}$, $\beta = 100$

$$f_T = \frac{1}{2\pi \tau_D} = 1.53 \text{ GHz}$$

$$f_B = \frac{f_T}{\beta} = 15.3 \text{ MHz}$$

$$11) \quad p_{E0} = \frac{n_i^2}{N_E} = 4.5 \times 10^2 / \text{cm}^3 \quad , \quad n_B(b) = n_{B0} \exp\left(\frac{V_{BE}}{V_T}\right)$$

$$n_{B0} = \frac{n_i^2}{N_B} = 2.25 \times 10^4 / \text{cm}^3 \quad = 2.25 \times 10^4 \exp\left(\frac{0.625}{26 \text{ mV}}\right)$$

$$p_{C0} = \frac{n_i^2}{N_C} = 2.25 \times 10^5 / \text{cm}^3 \quad = \underline{6.2 \times 10^{14} / \text{cm}^3}$$

$$12) \quad I_{nE} = 1.2 \text{ mA} \quad , \quad I_{pE} = 0.1 \text{ mA} \quad I_G = 0.001 \text{ mA}$$

$$I_{nC} = 1.18 \text{ mA} \quad , \quad I_R = 0.2 \text{ mA} \quad I_{pC} = 0.001 \text{ mA}$$

Find a) α b) δ c) $b(\beta_T)$ d) δ e) β .

$$\rightarrow \delta = \frac{I_{nE}}{I_{nE} + I_{pE}} = 0.923$$

$$\rightarrow b \text{ or } \alpha_T = \frac{I_{nC}}{I_{nE}} = 0.983$$

$$\rightarrow \delta = \frac{I_{nE} + I_{pE}}{I_{nE} + I_R + I_{pE}} = 0.867$$

$$\rightarrow \alpha = \delta b \delta = 0.7867$$

$$\rightarrow \beta = \frac{\alpha}{1 - \alpha} = 3.68$$

$$13) \quad W_B = 0.5 \mu\text{m} = 0.5 \times 10^{-4} \text{ cm} \quad , \quad D_B = 20 \text{ cm}^2/\text{s}$$

$$\tau_B = 0.2 \tau_{ec} \text{ or } (\tau_{ec})$$

$$\tau_b = \frac{W_B^2}{2D_B} = 6.25 \times 10^{-11} \text{ sec}$$

$$\tau_b = 0.2 \tau_{ec} \Rightarrow \tau_{ec} = \underline{3.125 \times 10^{-10} \text{ sec}}$$

$$f_T = \frac{1}{2\pi \tau_{ec}} = \underline{509 \text{ MHz}}$$