

Numericals on L, C, LC and pi Filters

Reference: Electronics Devices and Circuits 1 by Ravish Singh

Numerical 01

Example 5.1 Determine the ripple factor of an L-type choke input filter comprising a 10 H choke and 8 μF capacitor, used with a full wave rectifier. Compare with a simple 8 μF capacitor input filter at a load current of 50 mA and also 150 mA, assuming the dc voltage of 50 V.

Neglect the resistance of choke and assume supply of 50 Hz.

Solution :

$$L = 10 \text{ H}$$

$$C = 8 \mu\text{F}$$

For choke input filter,

$$\begin{aligned} \text{Ripple factor, } r &= \frac{1}{6\sqrt{2} \omega^2 LC} \\ &= \frac{1}{6\sqrt{2} \times (2\pi \times 50)^2 \times 10 \times 8 \times 10^{-6}} \\ &= 0.01492 \end{aligned}$$

For capacitor input filter, with $V_{\text{dc}} = 50 \text{ V}$ and $I_{\text{dc}} = 50 \text{ mA}$,

$$R_L = \frac{V_{\text{dc}}}{I_{\text{dc}}} = \frac{50}{50 \times 10^{-3}} = 1 \text{ k}\Omega$$

$$\begin{aligned} r &= \frac{1}{4\sqrt{3} fCR_L} \\ &= \frac{1}{4\sqrt{3} \times 50 \times 8 \times 10^{-6} \times 10^3} \\ &= 0.36 \end{aligned}$$

For $I_{\text{dc}} = 150 \text{ mA}$ and $V_{\text{dc}} = 50 \text{ V}$

$$\begin{aligned} R_L &= \frac{V_{\text{dc}}}{I_{\text{dc}}} = \frac{50}{150 \times 10^{-3}} \\ &= 0.33 \text{ k}\Omega \end{aligned}$$

$$\begin{aligned} r &= \frac{1}{4\sqrt{3} fCR_L} \\ &= \frac{1}{4\sqrt{3} \times 50 \times 8 \times 10^{-6} \times 0.33 \times 10^3} \\ &= 1.093 \end{aligned}$$

Thus for a choke input filter, ripple factor is 1.093 independent of load R_L whereas for a capacitor input filter, as load current increases, ripple factor increases.

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Numerical 02

Example 5.2 A full wave rectified voltage of 18 V peak is applied across a 500 μF capacitor. Calculate the ripple and dc voltage if the load current is 100 mA.

Solution :

$$V_m = 18 \text{ V}$$
$$C = 500 \mu\text{F}$$
$$I_{dc} = 100 \text{ mA}$$

For capacitor filter,

$$V_{dc} = V_m - \frac{I_{dc}}{4fC}$$
$$= 18 - \frac{100 \times 10^{-3}}{4 \times 50 \times 500 \times 10^{-6}}$$
$$= 17 \text{ V}$$

$$R_L = \frac{V_{dc}}{I_{dc}} = \frac{17}{100 \times 10^{-3}} = 170 \Omega$$

Ripple factor,

$$r = \frac{1}{4\sqrt{3} fCR_L}$$
$$= \frac{1}{4\sqrt{3} \times 50 \times 500 \times 10^{-6} \times 170}$$
$$= 0.03396$$

$$r = \frac{V_{r, rms}}{V_{dc}}$$

$$V_{r, rms} = 0.03396 \times 17$$
$$= 0.577 \text{ V}$$

Numerical 03

Example 5.3 A 100 μF capacitor when used as a filter has 15 V dc across it with a terminating load resistor of 2.5 k Ω . If the rectifier is a full wave and supply frequency is 50 Hz, what is the percentage of ripple in the output?

Solution :

$$C = 100 \mu\text{F}$$

$$V_{dc} = 15 \text{ V}$$

$$R_L = 2.5 \text{ k}\Omega$$

$$f = 50 \text{ Hz}$$

For capacitor filter,

$$r = \frac{1}{4\sqrt{3} fCR_L}$$

$$= \frac{1}{4\sqrt{3} \times 50 \times 100 \times 10^{-6} \times 2.5 \times 10^3}$$

$$= 0.01154$$

% of ripple in the output

$$= 0.01154 \times 100$$

$$= 1.154 \%$$

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Numerical 04

Example 5.5 A full wave rectifier circuit uses a capacitor filter with 500 μF capacitor and provides a load current of 200 mA at 8% ripple. Calculate

- (i) dc voltage across the filter capacitor
- (ii) the peak rectified voltage.

Assume the frequency of 50 Hz.

Solution :

$$\begin{aligned}C &= 500 \mu\text{F} \\I_{\text{dc}} &= 200 \text{ mA} \\f &= 50 \text{ Hz} \\r &= 0.08\end{aligned}$$

For capacitor input filter,

Ripple factor

$$\begin{aligned}r &= \frac{1}{4\sqrt{3}fCR_L} \\r &= \frac{I_{\text{dc}}}{4\sqrt{3}fC V_{\text{dc}}} \\V_{\text{dc}} &= \frac{I_{\text{dc}}}{4\sqrt{3}fC r} \\&= \frac{200 \times 10^{-3}}{4\sqrt{3} \times 50 \times 500 \times 10^{-6} \times 0.08} \\&= 14.43 \text{ V}\end{aligned}$$

$$\begin{aligned}V_{\text{dc}} &= V_m - \frac{I_{\text{dc}}}{4fC} \\V_m &= V_{\text{dc}} + \frac{I_{\text{dc}}}{4fC} \\&= 14.43 + \frac{200 \times 10^{-3}}{4 \times 50 \times 500 \times 10^{-6}} \\&= 16.43 \text{ V}\end{aligned}$$

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Numerical 04

Example 5.6 A power supply uses a full wave rectifier and LC filter with $L = 1.5 \text{ H}$ and $C = 500 \mu\text{F}$. It supplies 1 A to a 15Ω resistive load. Calculate the ripple voltage across the load.

Solution : For LC filter,

$$\text{Ripple factor } r = \frac{1}{5\sqrt{2}\omega^2LC} = \frac{1}{6\sqrt{2} \times (2\pi \times 50)^2 \times 1.5 \times 500 \times 10^{-6}}$$
$$= 1.59 \times 10^{-3}$$

$$r = \frac{V_{r, \text{rms}}}{V_{\text{dc}}}$$

$$V_{\text{dc}} = I_{\text{dc}} R_L = 1 \times 15 = 15 \text{ V}$$

$$1.59 \times 10^{-3} = \frac{V_{r, \text{rms}}}{15}$$

$$V_{r, \text{rms}} = 1.59 \times 10^{-3} \times 15 = 0.0238 \text{ V}$$